

$$\sin(x+y) = \cos(x)\sin(y) + \sin(x)\cos(y)$$

$$\cos(x+y) = \cos(x)\cos(y) - \sin(x)\sin(y)$$

$$\cos(2x) = \cos^2(x) - \sin^2(x)$$

$$\sin(2x) = 2\sin(x)\cos(x)$$

$$\cos^2(x) = \frac{1+\cos(2x)}{2} \qquad \sin^2(x) = \frac{1-\cos(2x)}{2}$$

$$\cos^2(x) + \sin^2(x) = 1$$

$$\cos(-x) = \cos(x) \qquad \sin(-x) = -\sin(x)$$

Substitution mit Hilfsvariable

$$\tan(x) = \frac{\sin(x)}{\cos(x)} \qquad \cot(x) = \frac{\cos(x)}{\sin(x)}$$

$$\tan(x) = -\cot(x + \frac{\pi}{2}) \qquad \cot(x) = -\tan(x + \frac{\pi}{2})$$

$$\cos(x - \frac{\pi}{2}) = \sin(x) \qquad \sin(x + \frac{\pi}{2}) = \cos(x)$$

$$\sin(x)\cos(y) = \frac{1}{2}\sin(x-y) + \frac{1}{2}\sin(x+y)$$

Für  $x \in [-1, 1]$

$$\arcsin(x) = -\arccos(x) - \frac{\pi}{2} \in [-\frac{\pi}{2}, \frac{\pi}{2}]$$

$$\arccos(x) = -\arcsin(x) + \frac{\pi}{2} \in [0, \pi]$$

| x                | deg  | cos(x)                | sin(x)               |
|------------------|------|-----------------------|----------------------|
| 0                | 0°   | 1                     | 0                    |
| $\frac{\pi}{6}$  | 30°  | $\frac{\sqrt{3}}{2}$  | $\frac{1}{2}$        |
| $\frac{\pi}{4}$  | 45°  | $\frac{\sqrt{2}}{2}$  | $\frac{\sqrt{2}}{2}$ |
| $\frac{\pi}{3}$  | 60°  | $\frac{1}{2}$         | $\frac{\sqrt{3}}{2}$ |
| $\frac{\pi}{2}$  | 90°  | 0                     | 1                    |
| $\frac{2}{3}\pi$ | 120° | $-\frac{1}{2}$        | $\frac{\sqrt{3}}{2}$ |
| $\frac{3}{4}\pi$ | 135° | $-\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{2}}{2}$ |
| $\frac{5}{6}\pi$ | 150° | $-\frac{\sqrt{3}}{2}$ | $\frac{1}{2}$        |
| $\pi$            | 180° | -1                    | 0                    |
| $\frac{3}{2}\pi$ | 270° | 0                     | -1                   |